

# MACHINE-LEARNING DRIVEN CORRELATION STUDIES: MULTI-BAND FREQUENCY CHIRPING AT NSTX

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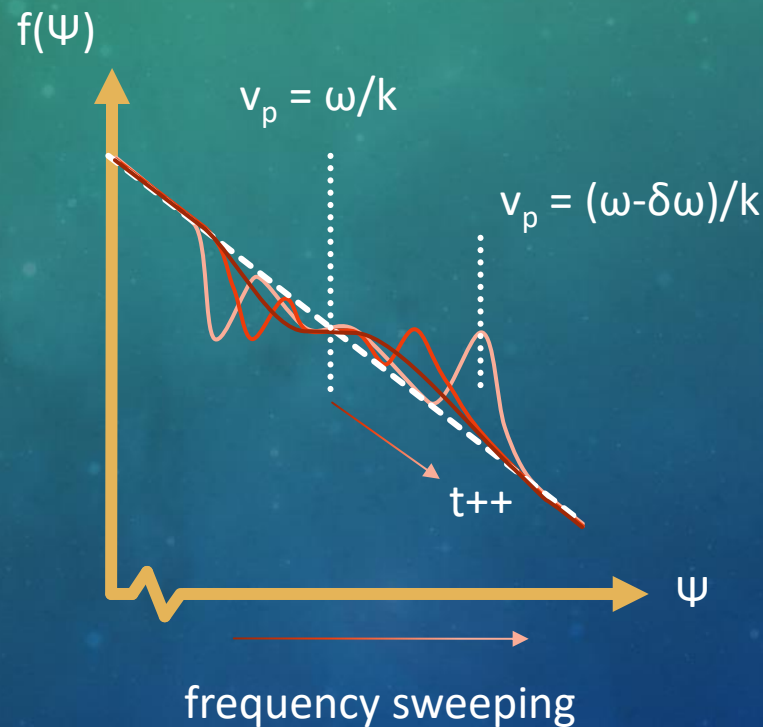
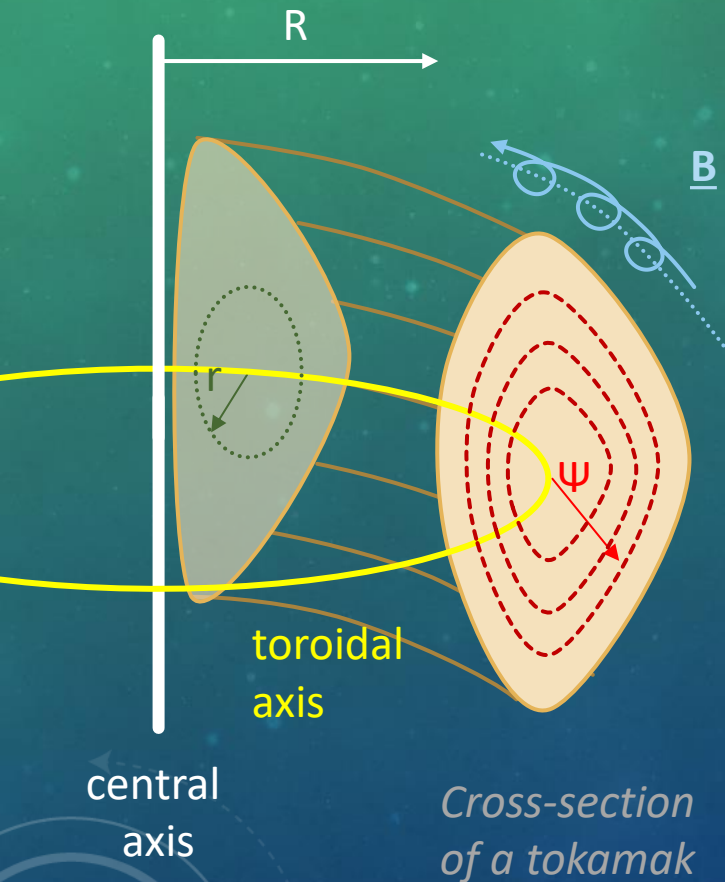
PPPL SEMINAR, 29.06.18

# SEMINAR CONTENT

- **Brief introduction to mode avalanching**
- **Machine learning for chirping characterisation**
- **Mode character correlations on NSTX**

# BRIEF INTRODUCTION TO MODE AVALANCHING

# FAST ION LOSS VIA RESONANT INSTABILITIES



## Resonant instability

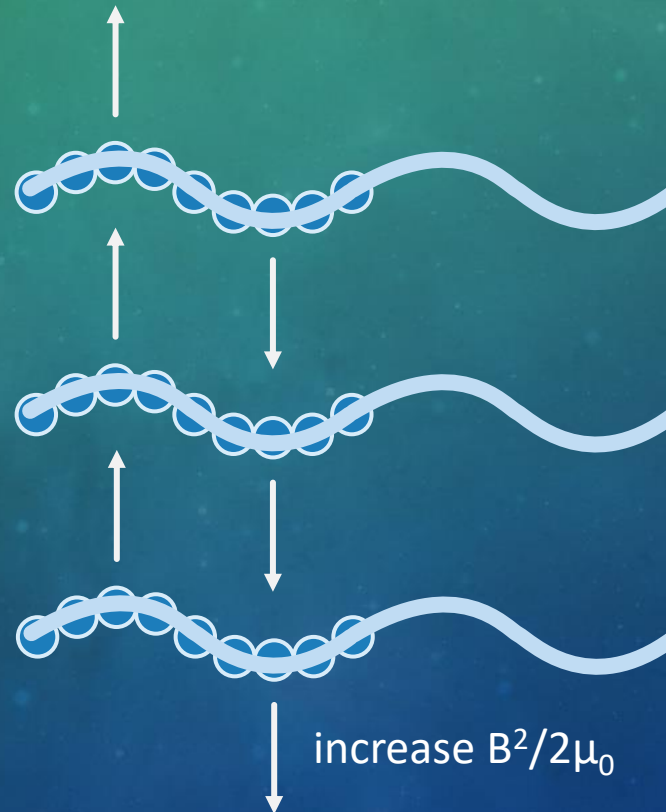
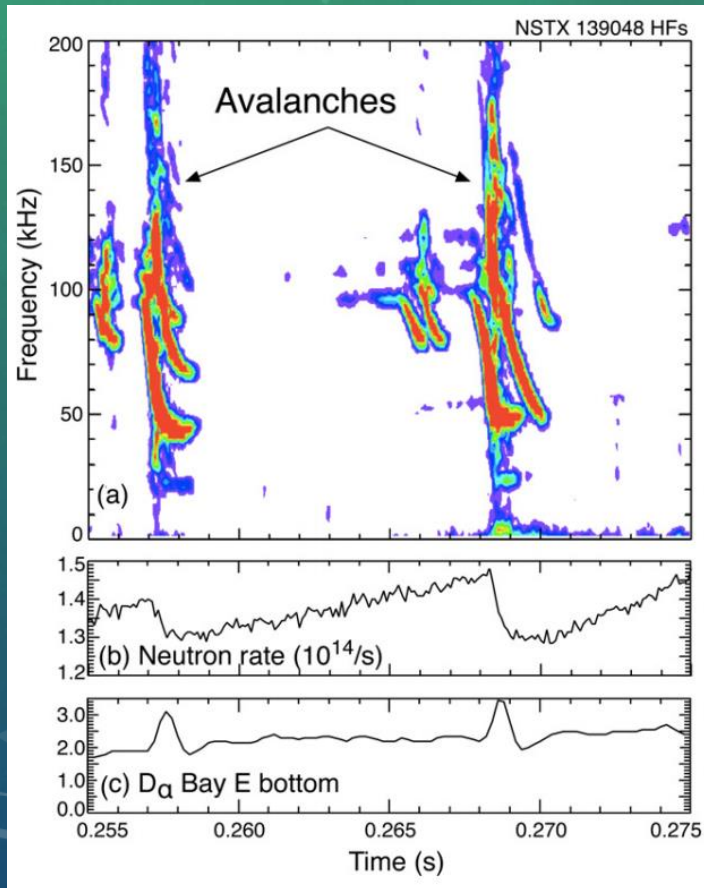
- Fast ion distribution is peaked near the toroidal axis
- Some particles resonate with the EM field (c.f. inverse Landau damping)
- **Frequency sweeping**
- **Fast ion transport mechanism**

$$p_\varphi = mRv_\varphi - q\Psi$$



# ALFVÉNIC AVALANCHING

Magnetic fluctuations from NSTX [1]



Alfvén waves

- MHD wave
- **Subject to kinetic instability**
- Compressional branch is analogous to acoustic wave

**Fast ion loss correlated with drop in neutron rate during “avalanches”**

**Research questions:**

?: What causes mode avalanching?

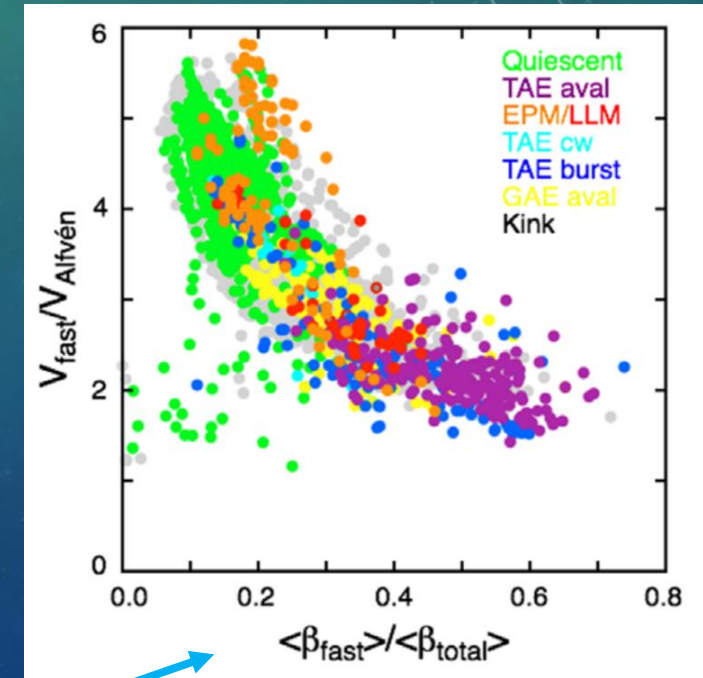
?: How can we stop it?

# MACHINE LEARNING FOR MODE CHARACTERISATION

# MACHINE LEARNING FOR FUSION APPLICATIONS

[2]

- Vast increase in speed for certain tasks
  - Data analysis can be done faster
  - Computational predictions can be extracted faster
  - May prove **vital** for operational performance of a tokamak
- Can we train an AI to recognise and characterise chirping?
  - Potentially feed into overall control system
- Knowledge of correlations between plasma parameters and mode character is **key**
  - i.e. turbulent suppression of mode chirping [3,4]



**very** time consuming to produce

only 2 parameters

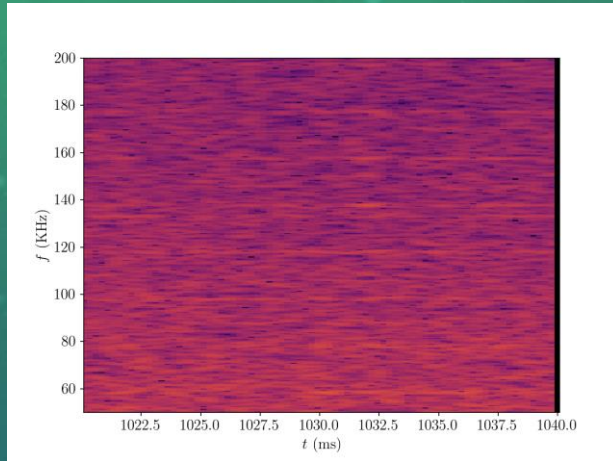
[2] E. D. Fredrickson *et al.* 2014 NF **54**, 093007

[3] V. N. Duarte *et al.* 2017 NF **57**, 054001

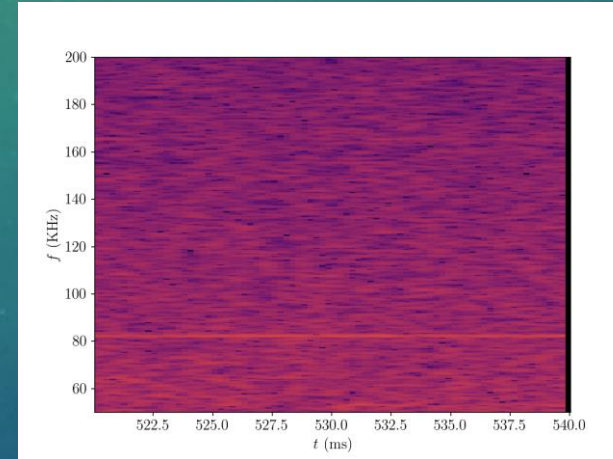
[4] B. J. Q. Woods *et al.* 2018 NF **58**, 082015



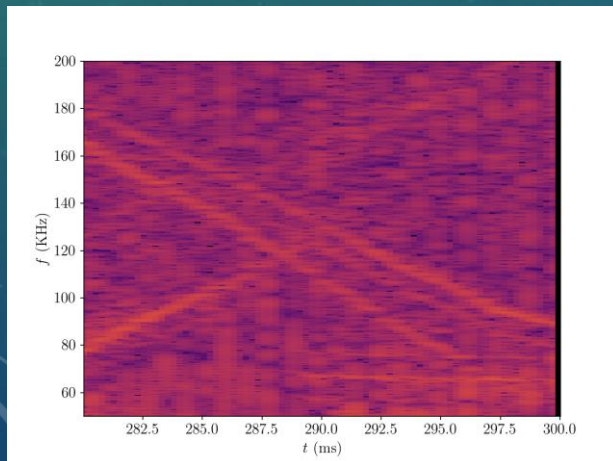
# MODE CHARACTER CATEGORIES



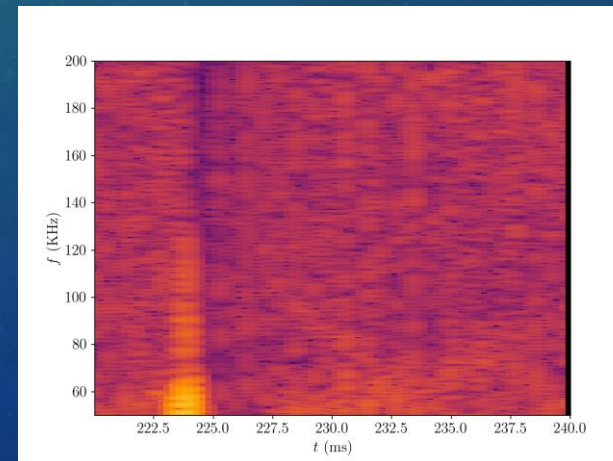
Noise/quiescence



Fixed frequency



Chirping



Avalanching

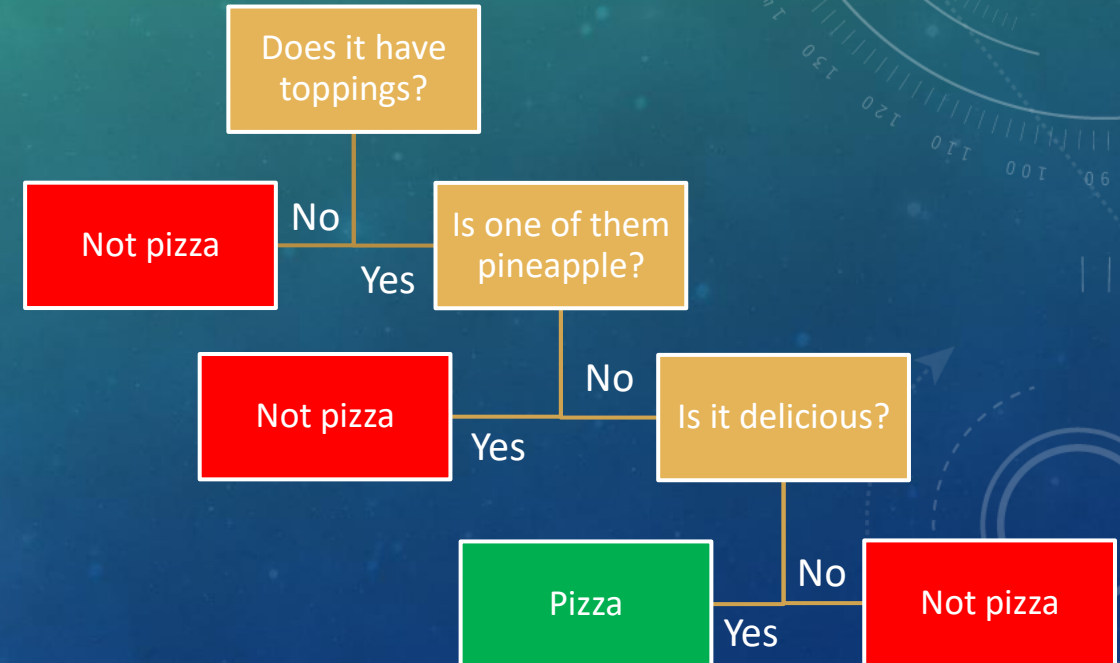
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# DECISION TREE CLASSIFICATION

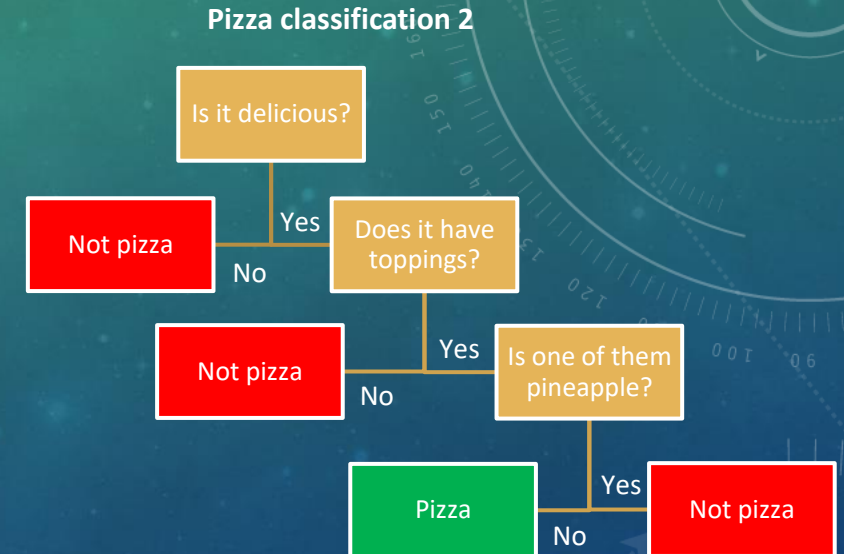
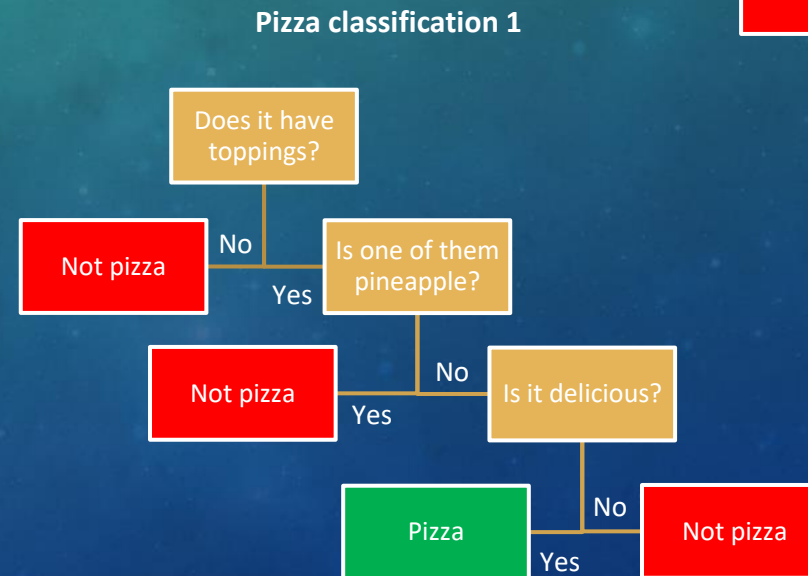
- Human classification can be broadly considered as a flowchart, or decision tree
- The maximum depth of the tree is the maximum number of decisions

## Pizza classification



# DECISION TREE CLASSIFICATION

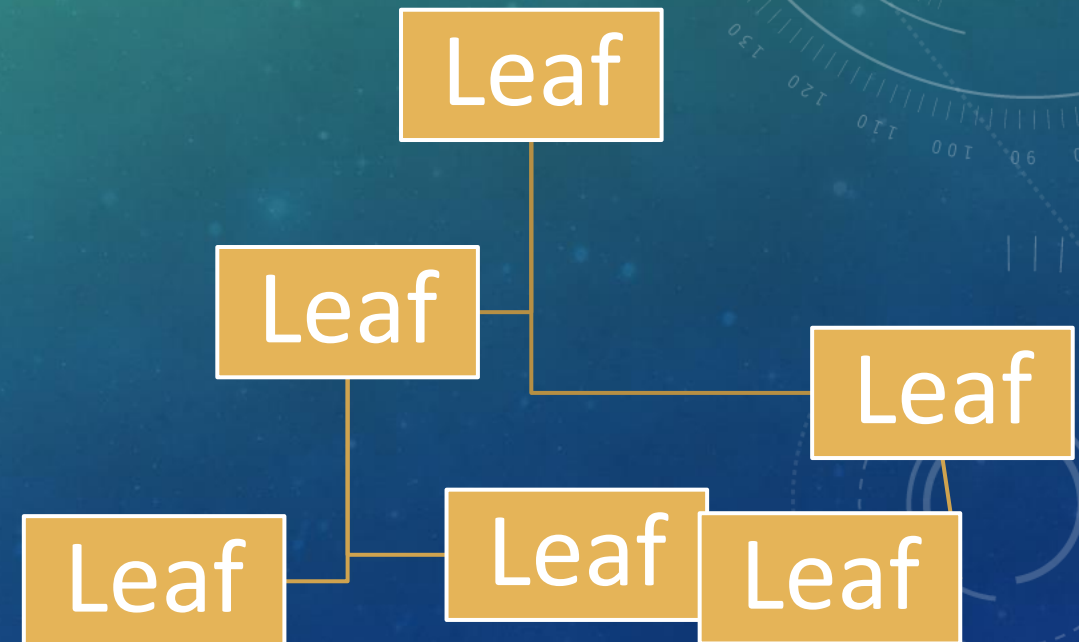
- In principle, there is a **free choice of decision tree**
  - We can ask different questions
  - We can permute questions
- Each tree **should lead** to the same overall outcomes



# DECISION TREE CLASSIFICATION

- A simple AI decision tree creates a “decision” (leaf), and places weights against the data
- After optimizing the weights by testing against the training set, it splits and creates more leaves based on probability of success
- Each branch (path between leaves) has a maximum depth
  - After training, the path taken through the tree depends on the found weights
- **Highly random structure**
  - Probability of successful classification varies from tree to tree
- Make the tree too deep - **overfit**
- Make the tree too shallow - **underfit**

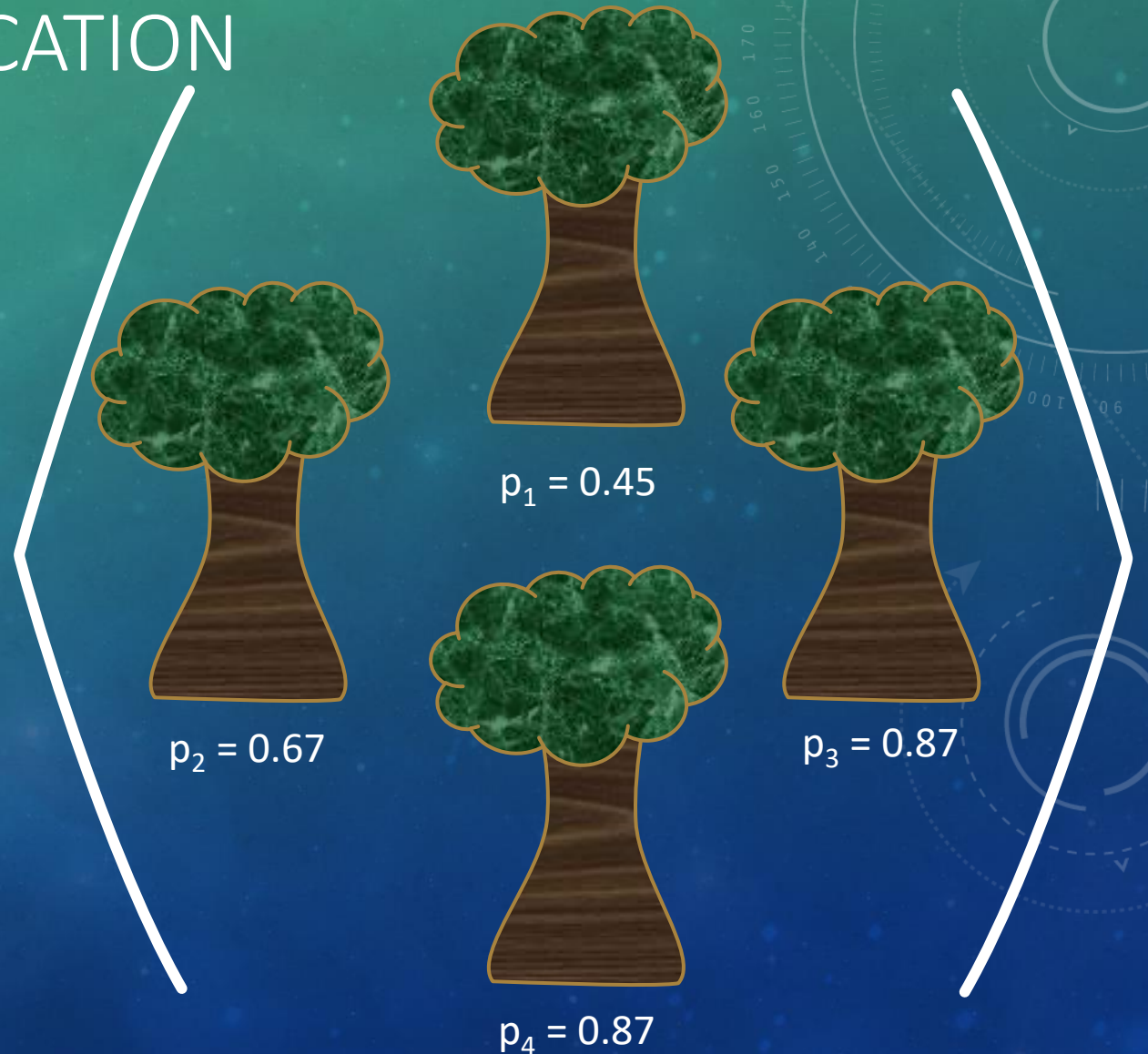
Pizza classification (AI)



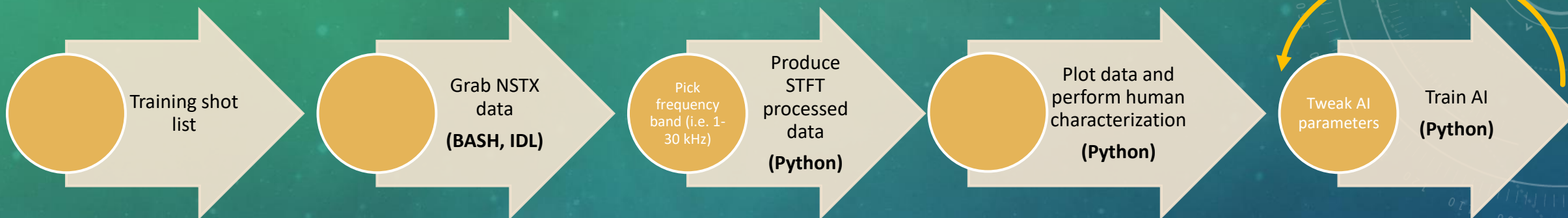


# RANDOM FOREST CLASSIFICATION

- Take an **ensemble** of trees, and take an average classification
- Linear average (mean) yields the mean accuracy
- Non-linear averages (mode, RMS) can yield higher accuracy than the mean
  - If the standard deviation in accuracies is low



# OVERALL TRAINING FRAMEWORK



[5]

The AI operates as a multi-class classifier:

- 4 **separate** classifiers (quiescent, fixed-freq, chirping, avalanching)
- Each classifier is a random forest in **scikit-learn**
  - Maximise probability by changing **no. of trees** and **branch depth (pruning)**
- Characterisation sits in a hierarchy (aval. > chirp. > fixed-freq. > quie.)

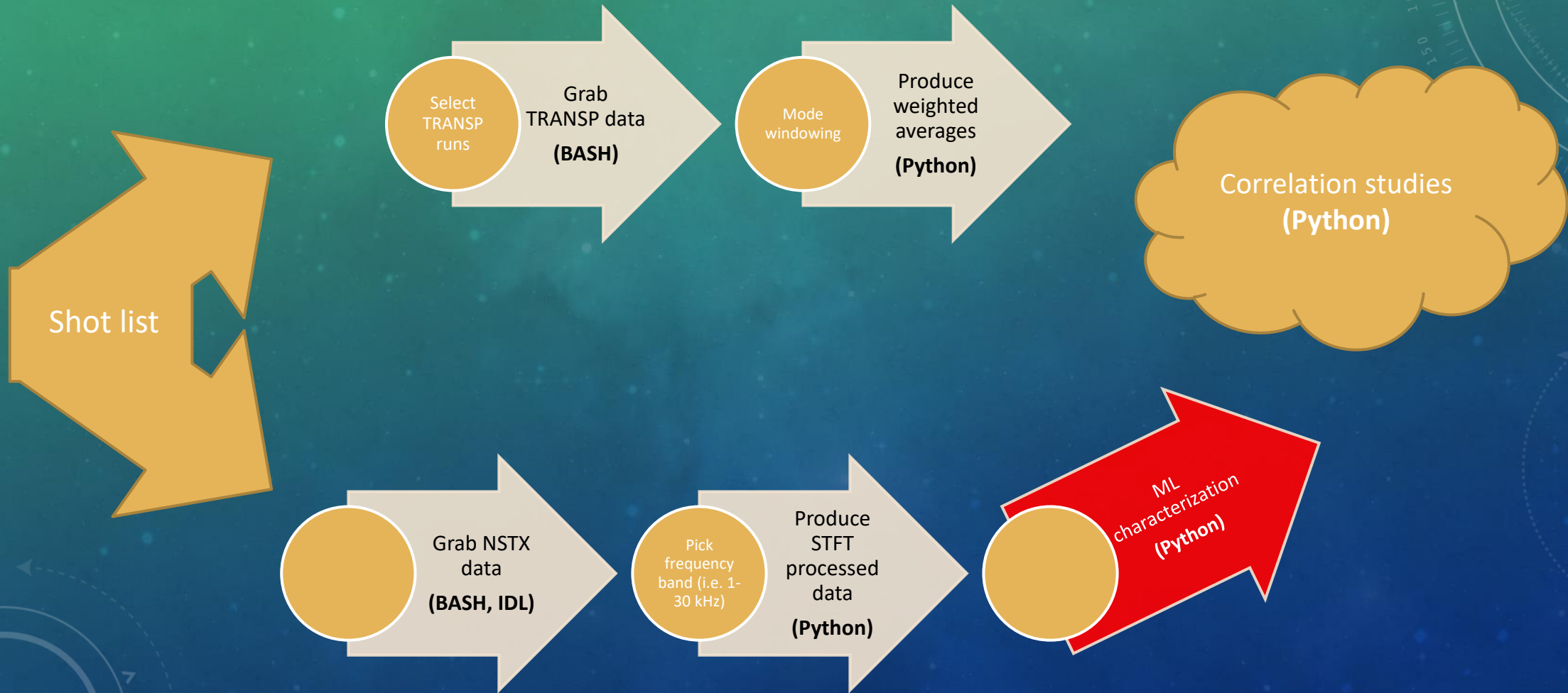
Take highest prob.

$$p \leq \max(p_i)$$

Take hierarchal prob.

$$p \leq \prod_{i=1}^4 p_i$$

# OVERALL CORRELATION FRAMEWORK

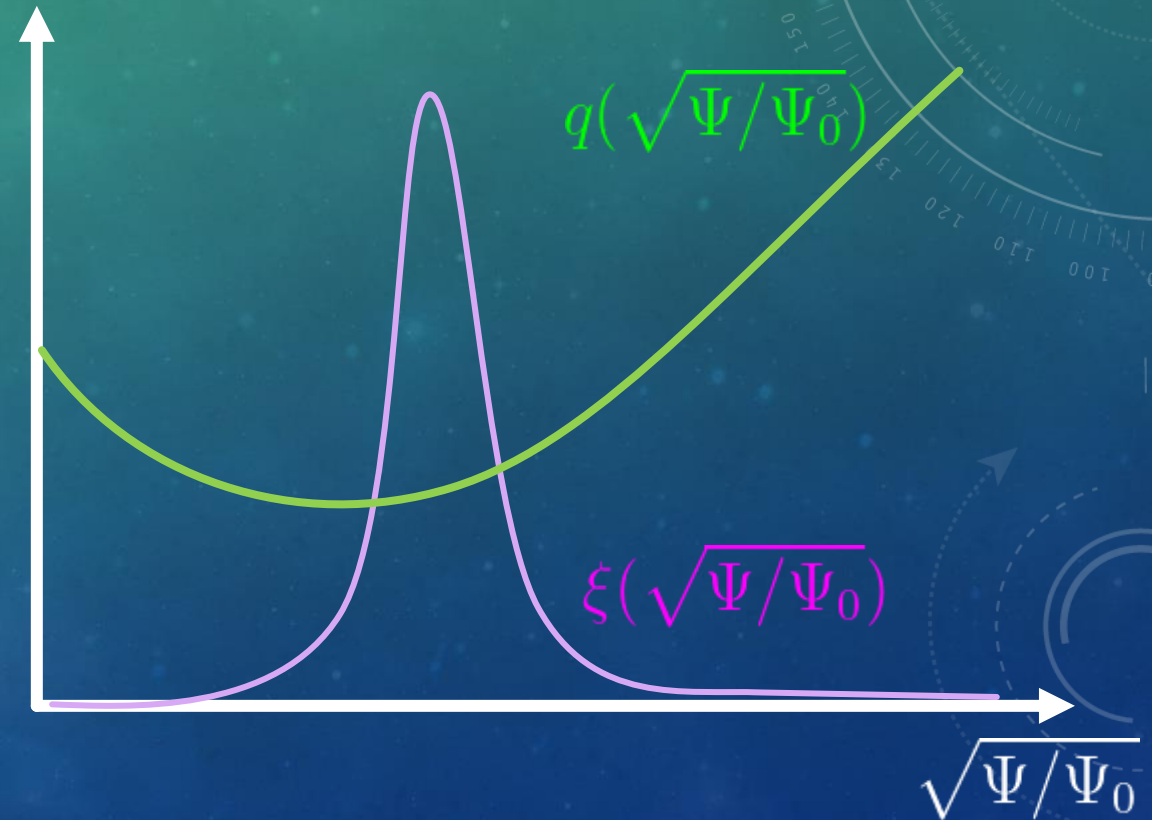




# WEIGHTED AVERAGES

- Chirping is a non-linear phenomenon
- Requires wave-wave or wave-particle nonlinearity
- **Aim:** correlate chirping with plasma parameters
  - These parameters can be spatially dependent
- **Solution:** take weighted averages
  - Weighting is a normalised 'window function' which mimics mode structure

$$\langle g \rangle \equiv \int_0^1 (g \cdot w) d\sqrt{\Psi/\Psi_0}$$



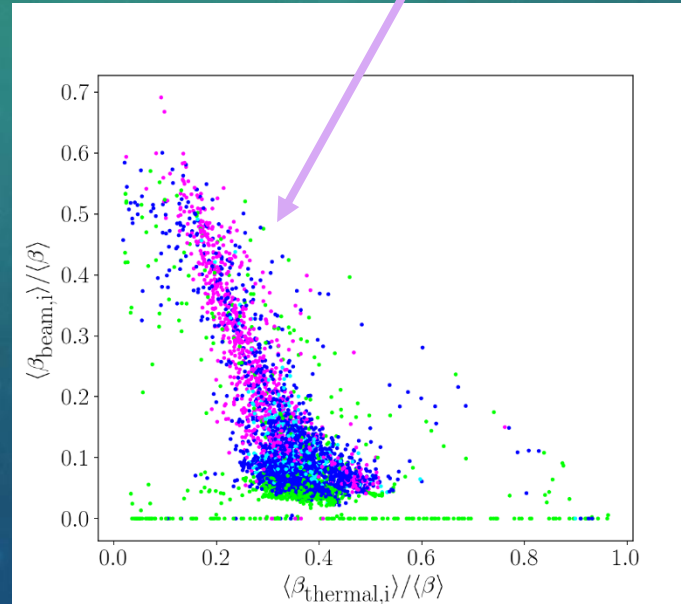
# BEAM ION BETA

*Measure of fast ion resonant drive*

- Low freq. modes:
  - Avalanche at high %
- TAEs:
  - Significantly less avalanching

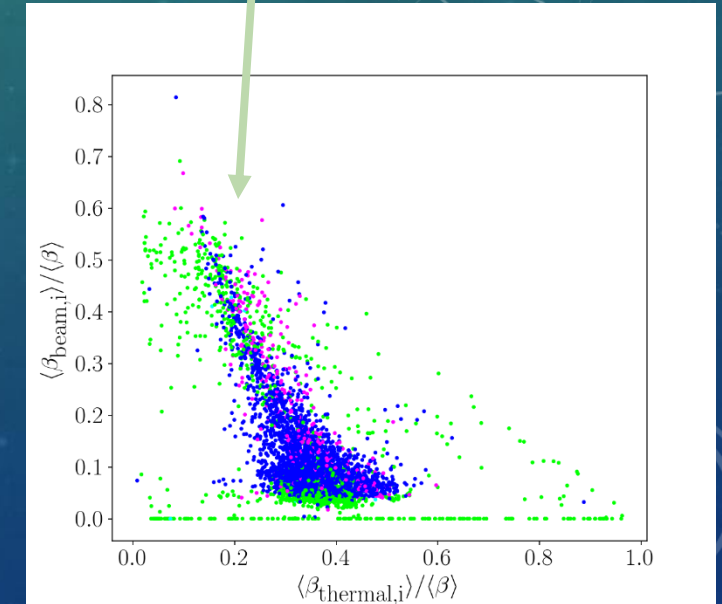
Generally at high beam ion beta,  
fishbones are very active while  
TAEs are less active

more avalanching



kink/tearing/fishbones  
(1-30 kHz)

more quiescence



TAEs  
(50-200 kHz)

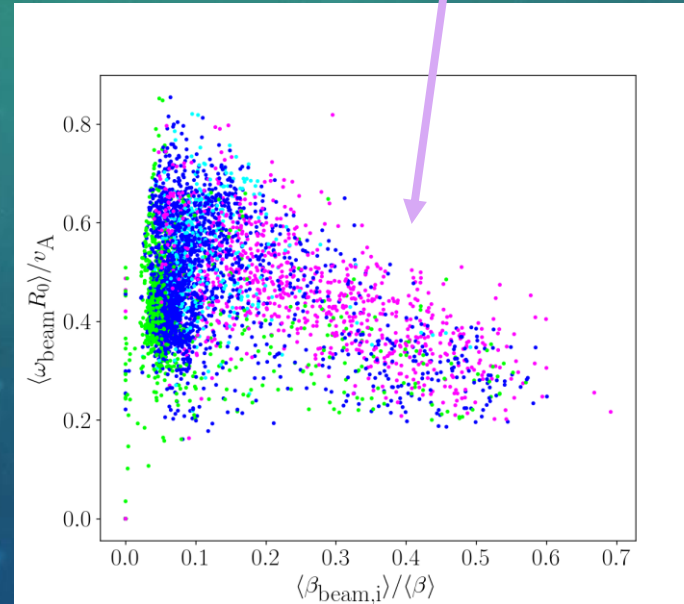
quiescent – fixed freq. – chirping – avalanching

# BEAM TOROIDAL VELOCITY

*Measure of fast ion average velocity*

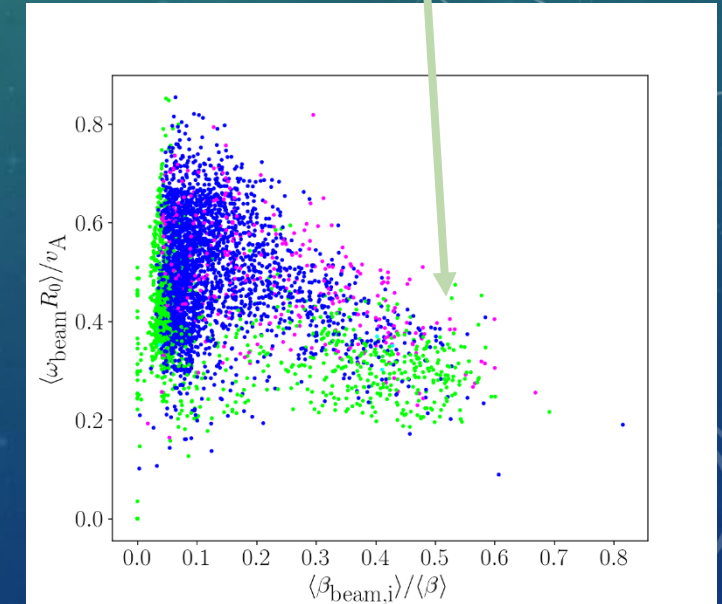
- Low freq. modes:
  - BTV not key factor for chirping
- TAEs
  - More quiescent at similar values of BTV for high beam ion beta

invariant w.r.t BTV



kink/tearing/fishbones  
(1-30 kHz)

slight preference w.r.t BTV



TAEs  
(50-200 kHz)

quiescent – fixed freq. – chirping – avalanching

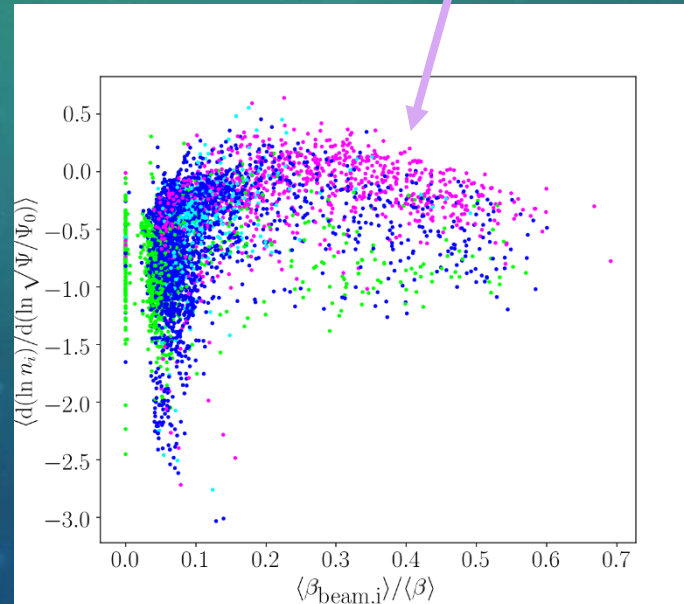


# NORMALISED ION DENSITY GRADIENT

*Measure of MHD stability*

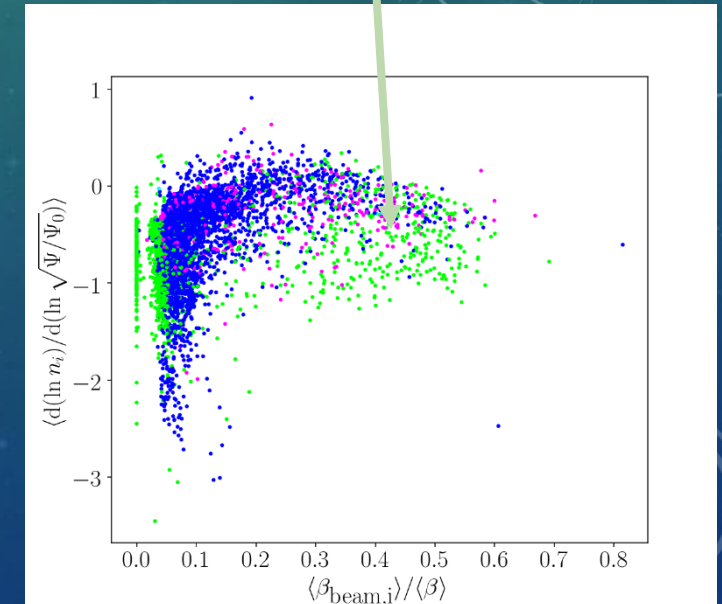
- Low freq. modes:
  - More avalanching/chirping at high beam beta
- TAEs:
  - More quiescence at high beam beta

more avalanching



kink/tearing/fishbones  
(1-30 kHz)

more quiescence



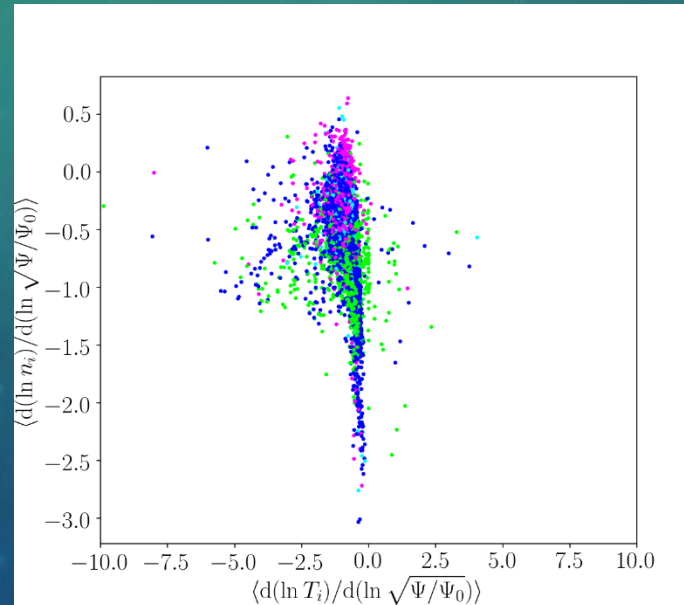
TAEs  
(50-200 kHz)

quiescent – fixed freq. – chirping – avalanching

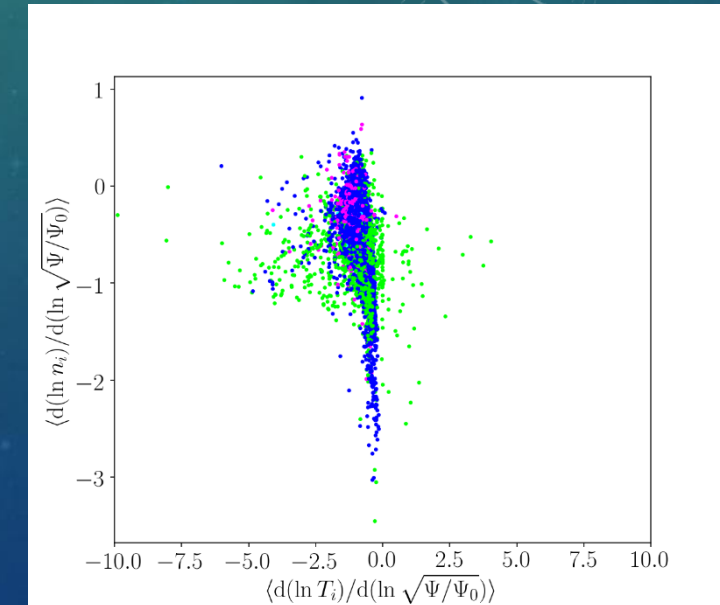
# TEMPERATURE AND PRESSURE GRADIENTS

*Measure of MHD stability*

- Both feature a window of increased quiescence
  - Modes here intermittently chirp
- At high  $|n_i'|$ , decreased quiescence
  - Modes here continuously chirp
- At  $n_i' > -0.5$ , increased avalanching?
  - Profile inversion/flattening due to large scale chirping/avalanching? (see [6])



kink/tearing/fishbones  
(1-30 kHz)



TAEs  
(50-200 kHz)

quiescent — fixed freq. — chirping — avalanching

# SUMMARY

- Particle resonance can lead to fast ion loss
- Machine learning offers a promising future for rapid characterisation of active modes in a tokamak
- Preliminary results show interesting correlations
  - Mode character depends strongly on beam beta
  - $|n_i'|$  may indicate hysteresis

*Thanks for listening!*